

Establishing bridges between UML, HAD and GRAFCET Metamodels for the Modelling of Dynamic Systems

M. Nkenlifack, E. Tanyi and F. Fokou

Abstract— This article shows the scope and limits of UML as a tool for modelling Automatic Control Systems. An alternative metamodel, Hybrid Activity Diagram (HAD), is proposed and applied to a concrete example, in order to illustrate its efficiency in comparison to the limits of UML diagrams. The article also presents bridges which interlink UML, HAD and GRAFCET and establish compatibilities between the three models. Specifications for the development of a HAD simulator and the results obtained from the implementation of the simulator, are also presented in the article.

Index Terms—HAD, UML, Grafcet, Hybrid Dynamic Systems, Modelling and Simulation.

1 INTRODUCTION

The Hybrid Activity Diagram (HAD) is a synthesis and fusion of concepts from two domains – Automatic Control Engineering and Software Engineering. The design and implementation of the formalism has been the subject of intense research [1], [2], [3], [4], [5]. The formalism is designed to model both the discrete and continuous parts of a system unlike single-paradigm tools like Grafcet [6] which model only one type of system.

Based on concepts of Object Orientation, HAD is designed to convert UML into a tool which is capable of modelling hybrid control systems, in order to facilitate the development of a simulator of such systems. In this regard, the focus of the article is to outline the design of HAD, as indicated in [1], [3], and to present its simulator which is known under the acronym SIMHAD. The functionality of SIMHAD is illustrated through an application which models and simulates a liquid-level control system. The model describes the causal relationships governing the operation of the system, the types of signals and the operational conditions of the system.

The primary advantage of the HAD metamodel is convertibility to both UML (Unified Modelling Language) and GRAFCET models through bridges which are described in the article.

The article is structured in six parts. Section 2 presents the fundamental concepts associated with hybrid systems and UML. The modelling of a liquid-level control system using UML is then presented in section 3 and this serves as a springboard for understanding and defining the properties of HAD. The bridges or mechanisms for converting the HAD model into Grafcet and UML Activity Diagram are presented in section 4. The specifications of the hybrid simulator SIMHAD and the results obtained from the simulation of the liquid-level control system are presented in section 5. The last part of the article, section 6, presents the conclusions and perspectives for further work.

2 HYBRID DYNAMIC SYSTEMS AND UML FUNDAMENTALS

A hybrid dynamic system is one which incorporates both continuous and discrete subsystems. The continuous subsystems are characterized by continuous-time variables while the discrete subsystems are event-driven and usually sequential in operation. More ample information on such systems can be obtained in [1], [3], [7], [8], [9]). A hybrid dynamic system can, thus, be represented as shown in figure 1.

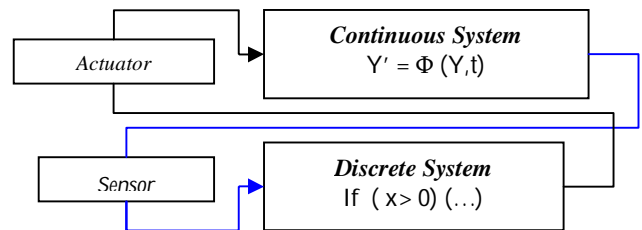


Fig. 1. Structure of Hybrid Dynamic Systems [9]

When the logic condition defined on the variable X is true, the actuator immediately triggers the operation ($Y' = \Phi(Y, t)$), resulting in a "sequential - continuous" interaction between the discrete and continuous subsystems [2]. When the continuous subsystem executes the specified action, this is detected by the sensor which provides information on the state or status of the actuator and the sequential subsystem is switched to the next state of the sequence. The result is a "continuous-sequential" interaction [2].

A hybrid dynamic system is, thus, characterized by interactions between the continuous and discrete subsystems. The evolution of the discrete subsystem from one state to another is predicated on the state of the logic va-

riables while the operation of the continuous component is based on physical laws which are usually described by differential or algebraic equations expressing cause-and-effect relationships. However, most of the tools and paradigms developed for the modeling and simulation of dynamic systems are either continuous or discrete ([1], [3], [8], [10]).

The primary focus of this research project is, therefore, to model and simulate hybrid dynamic systems using the Unified Modeling Language (UML) which is a universal, implementation-independent modeling language providing such properties as modularity, structured programming, re-usability and extensibility [11]. Based on Object Orientation, UML provides a multiplicity of diagrams which can be used to define the inheritance of attributes between related classes of objects as well as relationships between the components of a system [3], [11] [10].

3 ANALYSIS OF A LIQUID-LEVEL CONTROL SYSTEM TO HIGHLIGHT THE LIMITS OF UML

3.1 System Functionality

The system in figure 2 is taken from [12]. Each of the two tanks is fitted with two sensors, one of which detects when the tank is empty and the other detects when the tank is full. Sensor b1, in tank 1, detects when tank1 is empty while sensor h1 detects when the tank is full. Similarly, b2 and h2 have the same functions in tank 2. The sensors are, therefore, level-detectors and are modeled as binary rather than continuous variables.

The sequence of operations is as follows:

- Initially, both tanks are empty
- When the operator presses the switch *m*, the inlet valves *V1* and *V2* open and the tanks start filling up
- Once a tank is full, the corresponding inlet valve (*V1* or *V2*) closes, to stop filling the tank, and the corresponding outlet valve (*W1* or *W2*) opens, to start evacuating the contents of the tank.
- When a tank is empty, the corresponding outlet valve is closed

When both tanks are empty, the sequence repeats, to start refilling the tanks, when the operator presses the button *m*.

3.2 Modeling of the system using UML

3.2.1. Analysis of system functionality

The system functionality described in section 3.1 requires the following Use-cases: starting the system, opening of the valves (*V1*, *V1*, *W1*, *W2*), activation of the sensors (*h1*, *h2*, *b1*, *b2*), filling of the tanks and evacuation of the contents of the tanks. The actors include the operator, motor and tank, for each filling operation.

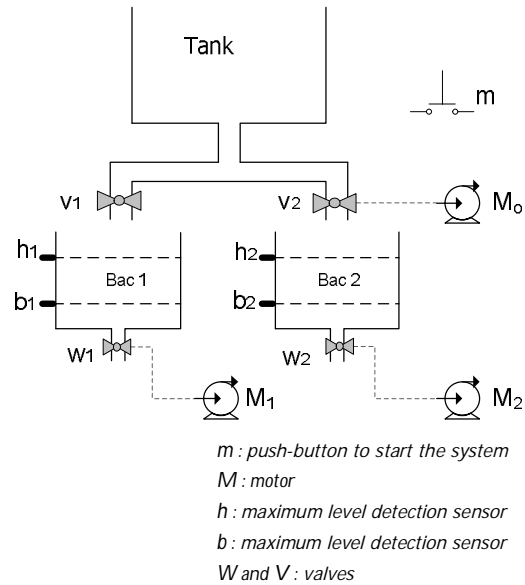


Fig. 2. Liquid-level control system [12].

The Use-case diagram (a fundamental UML construct for the description of the functions of a system), which associates the actors to their actions, is shown in figure 3.

This Use-case diagram shows the different sequences and highlights the role of each actor.

3.2.2. Other UML Diagrams required for the Modeling of the System

The Diagram of Classes in figure 4 shows both the static links between the actors as well as the action associated with each link.

The Diagram of Classes in figure 4 describes the attributes of the system components and the communication between them, but it does not describe the sequence of execution of the various tasks, neither does it define the conditions associated with the different tasks as is commonly the case with control systems modeling tools such as Grafcet and Petri nets. For this reason, Sequence Diagrams are required to describe the chronology in task execution. However, in order to avoid any ambiguity, more detailed description of the sequences are required.

We consider two scenarios.

Scénario 1 : Sequence of actions in the filling of tank 1

- When the system operator presses the button *m*, motor *Mo* is turned on.
- When motor *Mo* reaches its operational speed, it opens the inlet valve *V1*, to start filling tank 1.
- When tank 1 is full (*h=1*), motor *Mo* reverses its direction of rotation. *Mo* is, thus, a bi-directional motor.
- Motor *Mo*, rotating in the reverse direction, closes the inlet valve *V1*.

The Sequence Diagram for this sequence of operations is shown in figure 5.

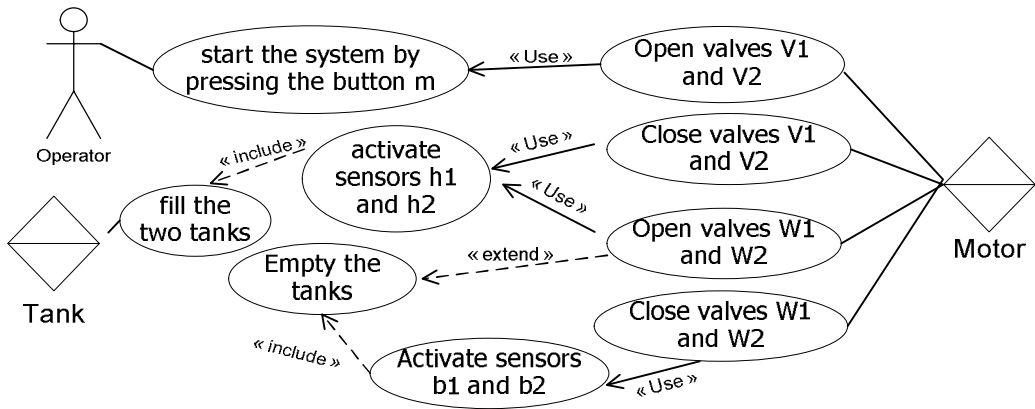


Fig. 3. Use-case diagram of the liquid-level control system

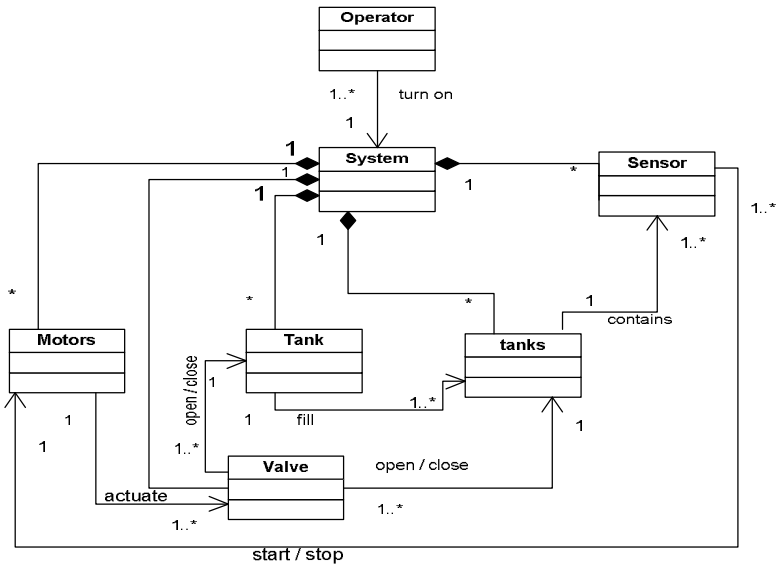


Fig. 4. Diagram of Classes of the liquid-level System

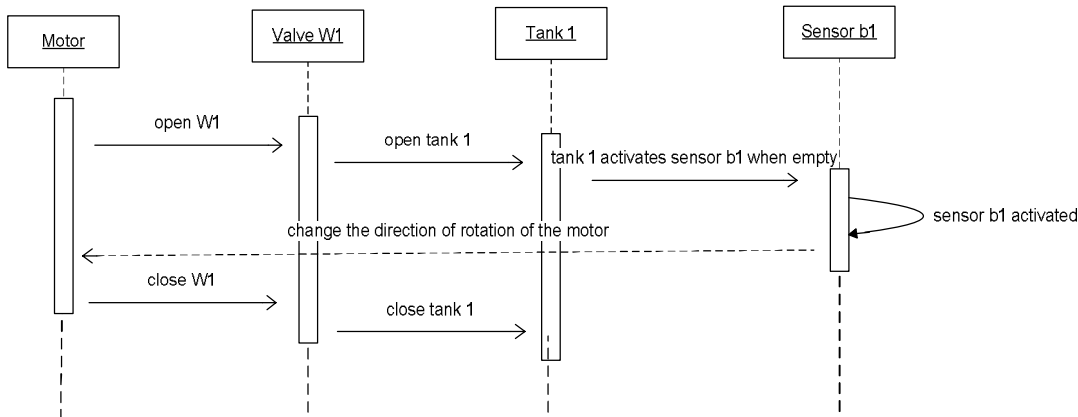


Fig. 5. Sequence Diagram for the filling of tank 1

Scénario 2 : Sequence of actions in the evacuation of the contents of tank 1

1. The activation of sensor h1 (last step in scenario 1) turns on motor M1
2. Motor M1 opens the outlet valve W1 for evacuation of the liquid
3. When tank 1 is empty ($b1=1$), motor M1 reverses its direction of motion
4. The rotation of M1, in the reverse direction, closes valve W1.

The corresponding Sequence Diagram is shown in figure 6.

The two Sequence Diagrams (figures 5 and 6) provide detailed information on the order in which the different actions are executed during the filling and evacuation of the contents of tank 1. These Sequence-diagrams are also valid for tank 2, by simply substituting the variables of tank 1 with those of tank 2. However, they do not describe sequence selection and simultaneous (parallel) sequences. The appropriate structure for such sequences is the Activity Diagram [3],[11]. Figure 7 presents the Activity Diagram for the overall system functionality involving the filling and evacuation of the contents of the two tanks.

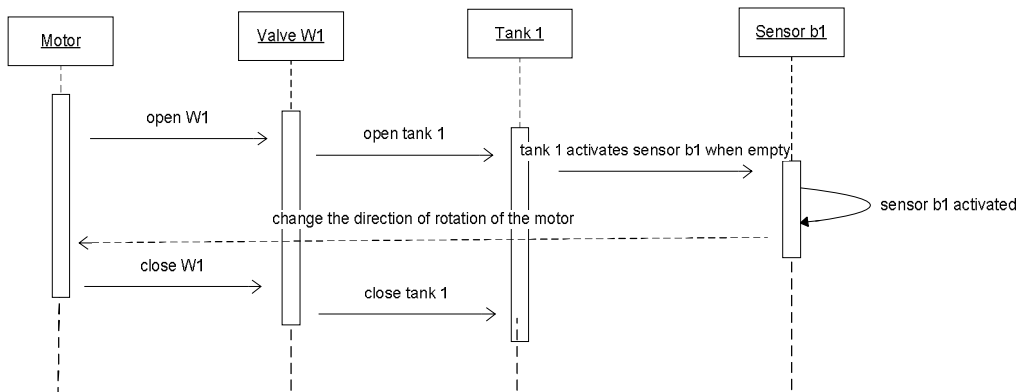


Fig. 6. Sequence Diagram for the evacuation of the contents of tank 1.

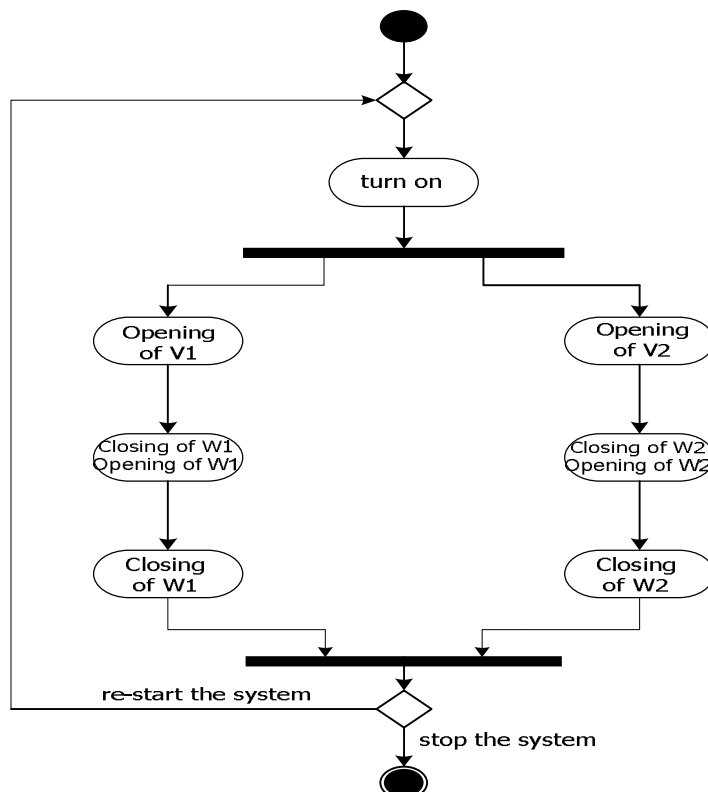


Fig. 7. Activity Diagram for the overall system functionality involving the filling and evacuation of the contents of the two tanks

The diagram in figure 7, in addition to combining the information in figures 5 and 6, shows the conditions for

simultaneous and conditional activation of sequences as well as the order of execution of the actions in a sequence. However, the conditions (state of the sensors) driving the sequence from one state to another, are not shown.

The various limits of UML highlighted in its application to the modeling of the liquid-level system confirm the assertion in [1], [2] that UML does not model the cause-and-effect phenomena in dynamic systems. This creates the need for the HAD metamodel which allows sequences to be modeled as Object-oriented entities incorporating cause-and-effect relationships and the capacity to interchange messages between objects.

4. EXTENSION OF UML TO THE MODELING OF HYBRID SYSTEMS: APPLICATION TO THE LIQUID-LEVEL SYSTEM

Inspired by the Activity Diagram [4], [11], [13], HAD is designed to model a system as a collection of localized, autonomous objects having both static and dynamic properties and incorporating a representation of the physical phenomena associated with an object. For the most part, the phenomena are described by differential equations, but algebraic and logic equations are sometimes used.

4.1. Analysis of the filling of the two tanks

The opening of a valve requires the actuation of the valve stem by the motor. The motion of the motor, coupled to the valve stem, is described by:

$$\frac{J_t}{f_r} \frac{d\Omega}{dt} + \Omega = \frac{T_{em} - T_r}{f_r} \quad (1)$$

And the electromagnetic torque which drives the motor shaft and valve stem is given by :

$$T_{em}(n) = K \cdot V_1^2 \cdot \frac{-(R_2 \cdot n_s)n + R_2 n_s^2}{X_2^2 \cdot n^2 - 2(n_s \cdot X_2^2)n + n_s^2(R_2^2 + X_2^2)} \quad (2)$$

Where,

f_r frictional torque constant ;

J_t is the combined moment of inertia of the motor shaft and load ;

R_2 and X_2 are the resistance and reactance of one phase of the motor ;

n_s is the synchronous speed

Details of these equations are available in [17].

The block diagram in figure 8 regroups and organizes the causes and effects of the system into a single entity. The sensors and push-button "m" are the causes while the valves which are the controlled components are the effects.

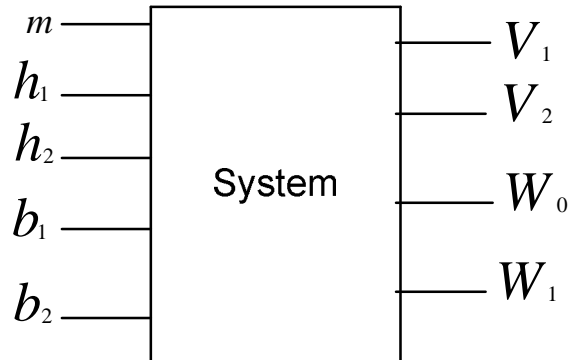


Fig. 8. Block Diagram for the filling of the two tanks

The corresponding HAD diagram is shown in figure 9.

The HAD diagram is an abstract representation of the filling process and provides a more realistic description of the system since there is greater visibility of the signals (discrete and continuous) interchanged and a better expression of the alternation between the sequential and continuous subsystems. Consequently, it describes the physical phenomenon (through equations) which govern the behavior of the system. It also facilitates the analysis of the system at three levels : visual, syntactic and semantic. This, in turn, facilitates the development of the simulation model.

4.2. Bridges between HAD and other Metamodels

The bridges are pre-defined rules which are embedded in the HAD diagram for the automatic generation of equivalent UML or Grafcet models. Since this article is not entirely devoted to these bridges, only a subset of these rules and their implementation will be presented here.

4.2.1. The HAD – UML Bridge

Table 1 presents an excerpt of the rules for converting a HAD model to UML.

These rules of conversion have been successfully tested on several systems ([14], [15], [5]). The application of the rules to the HAD diagram in figure 9 generates the Activity Diagram in figure 10, which conforms to the UML formalism [13].

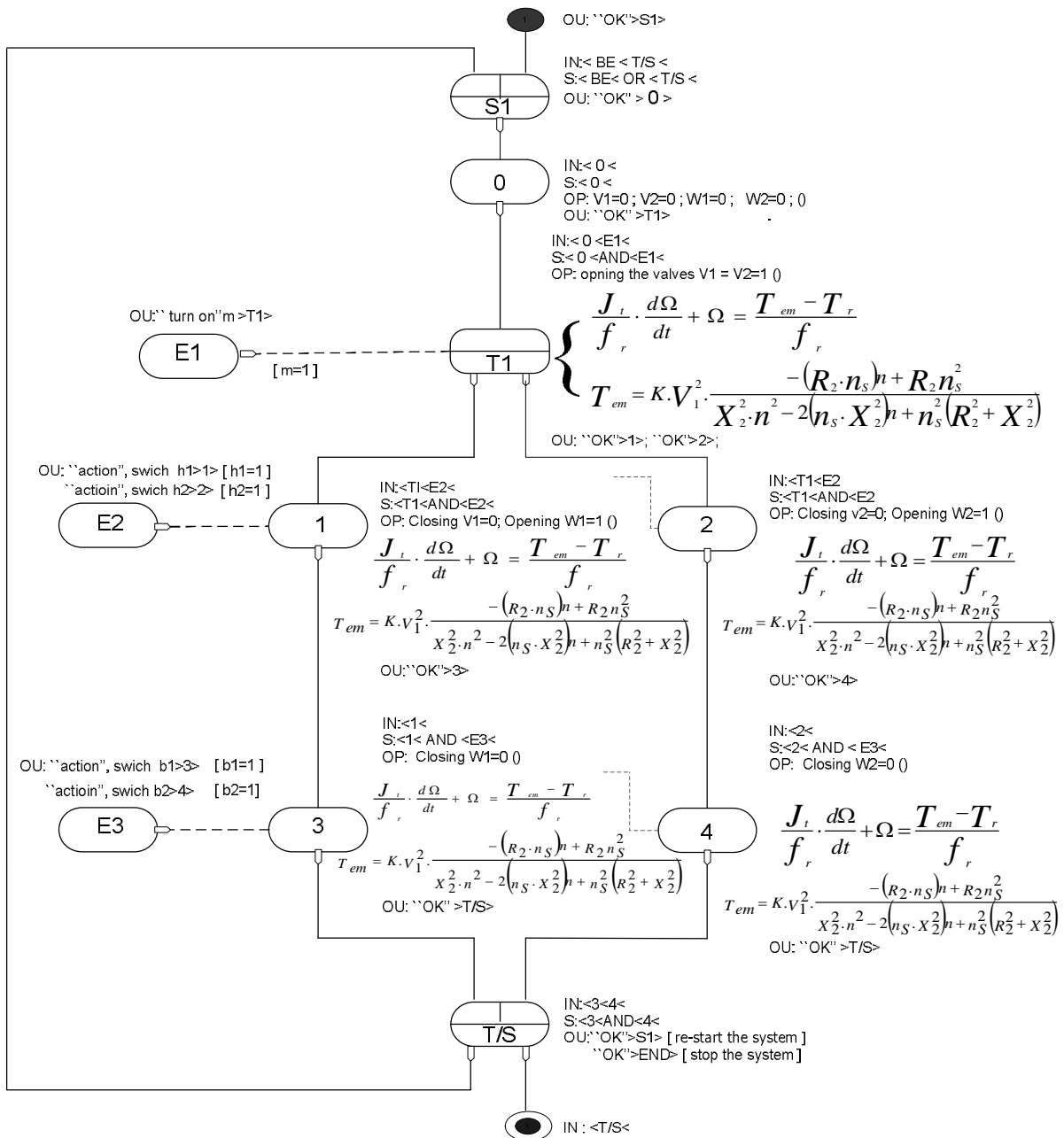
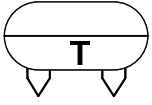
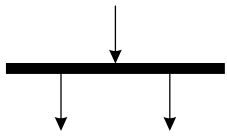
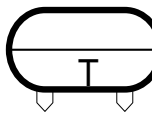
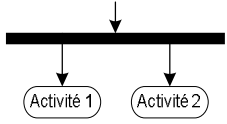
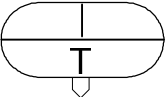
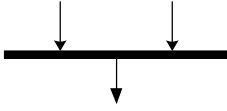
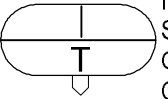
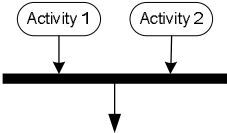
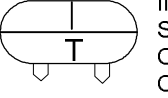
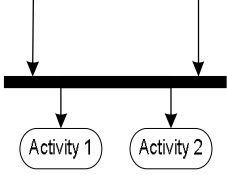
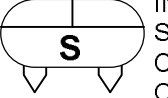
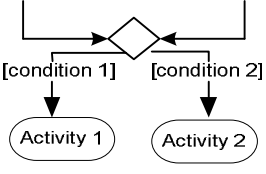
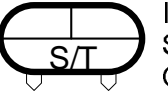
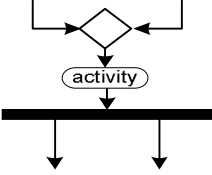
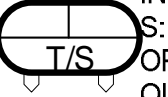
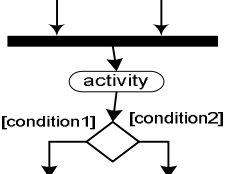


Fig. 9. HAD Model for the filling of the two tanks

TABLE 1
EXCERPT OF THE RULES USED IN CONVERTING HAD MODELS TO UML

Beginning of simultaneous sequences: "AND" - divergence	 <p>IN: S: OU:</p>	Object without an operation	
	 <p>IN: S: OP: op1 (), op 2 () OU:</p>	Object with operation (op 1 and op 2 become activity 1 and activity 2 respectively)	

End of simultaneous sequences : "AND" - convergence	 IN: S: OU:	Object without an operation	
	 IN: S: OP: op1(), op2() OU:	Object with operation (op 1 and op 2 become activity 1 and activity 2 respectively)	
"AND" - divergence and convergence	 IN: S: OP: op1(); op2() OU:	If there is no operation, the two activities after the bar are deleted	
"OR" - divergence and convergence	 IN: S: OP: op1(), op2() OU: >'ok'> [garde 1] >'ok'> [garde 2]	If there is no operation, the activities which are present are deleted	
"OR" - convergence "AND" - divergence	 IN: S: OP: opération() OU:	If there is no operation, the activity which figures on the object is deleted	
"AND" - convergence "OR" - divergence	 IN: S: OP: opération() OU: >'ok'> [garde 1] >'ok'> [garde 2]	If there is no operation, the activity which figures on the object is deleted	

4.2.2. The HAD – Grafcet Bridge

The HAD-Grafcet bridge is designed to perform a two-stage transformation. The HAD source-code is first transformed into an intermediate model, which is then transformed into Grafcet

Intermediate Model for the transformation of HAD into grafcet

Only an excerpt of rules is presented here. More details of the relationships between the two metamodels are presented in [14], [15].

- Eliminate the object which marks the beginning and end of the HAD metagraph
- Eliminate all mathematical equations assigned to the attribute "operation" which describes the dynamics of an object

External influences (ActivityCauses, ActivityEffects) and internal influences (ActivityClasses) to which the

system is subjected are equivalent to conditions on Grafcet transitions.

Transformation of Intermediate Model into Grafcet

An excerpt of the rules in [14], [15] is presented here. Analyzing the Grafcet from top to bottom :

- Delete all parallel or conditional sequences (sequence selection) which do not have steps between them ;
- Merge any two consecutive transitions which are not separated by a step

The application of this bridge to the HAD model for the filling of the two tanks generates the Grafcet in figure 11, which conforms to the Grafcet principle of the alternation of steps and transitions.

These models illustrate the fact that HAD models provide greater visibility and abstraction of actions, operations and interchange of signals of a hybrid dynamic sys-

tem, compared to the other modeling paradigms used in Automatic Control Engineering. HAD extends UML and adapts it to the requirements of Automatic Control Engineering. This property makes it an interesting tool. In the

next section, we show that its syntax and structure facilitate the development of software for the simulation of hybrid dynamic systems.

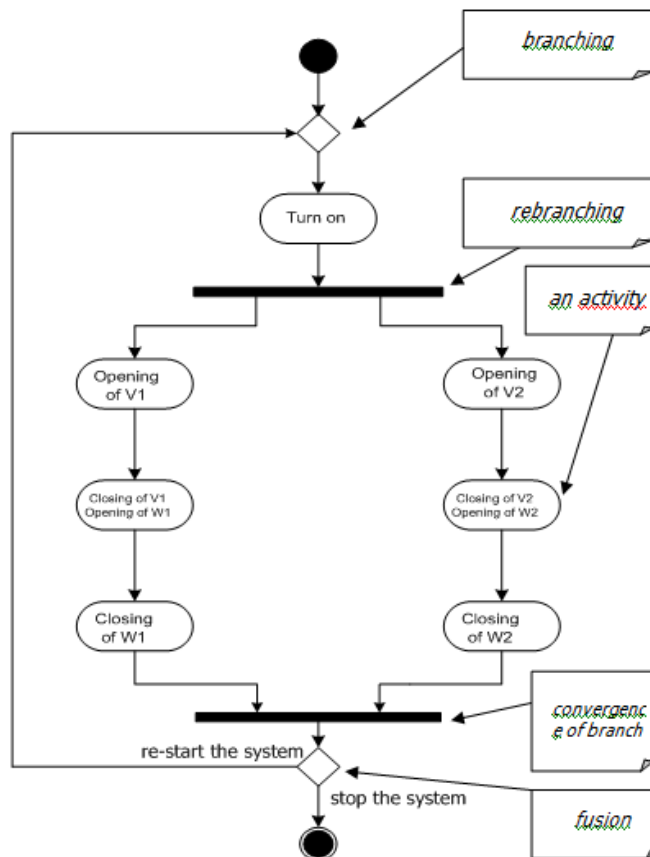


Fig. 10. Activity Diagram generated from the HAD model for the filling of a single tank.

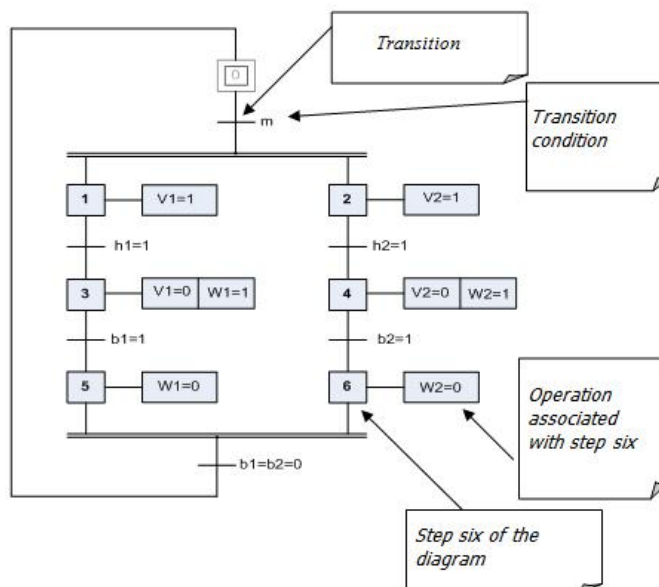


Fig. 11. Grafcet generated from the HAD model for the filling of two tanks,

5. TECHNICAL SPECIFICATIONS AND ABSTRACT

HYBRID SIMULATION OF SYSTEMS

5.1. Technical Specifications

The HAD metamodel has the advantage of being an extension of UML which is widely used in software engineering [13]. This is the motivation and justification for the development of a simulator of HAD models.

This aspect requires a specification of dozens of constraints. Some of these constraints are highlighted in this section. The full details are available in [14], [15].

5.1.1. Constraints on the Structure of HAD Models

- CH 1: An object is either active or inactive at any given time.
- CH 2: An object is associated with one or more operations.
- CH 3: Two objects communicate through influences (sending and reception of messages) which are either internal or external.
- CH4: An object can be subjected to internal and external influences at the same time. This is a corollary of CH3.
- CH 5: The alternation of transmission and reception of influences must be observed at all times.

- CH 6: The initial and terminal objects must be at the appropriate places.

5.1.2 Constraints on the interconnection of objects:

- CH 7: The ActivityCause – ActivityClass or Activity-NoEffect must be represented as horizontal dotted lines.
- CH 8: The ActivityEffect – ActivityClass or Activity-NoEffect must equally be represented as horizontal dotted lines.
- CH 9: The links between the objects : ActivityClass, ActivityNoeffect, ActivitySelect, ActivityThread, ActivitySelect/thread, ActivityThread/Select, must be represented as vertical solid lines.

5.1.2. Constraints on the description of entities

- CH 10: All objects are inactive during their description.
- CH 11: The order of a differential equation must be greater than or equal to 1.
- CH 12: Algebraic equations are valid if and only if their coefficients are correct.
- CH 13: The fields reserved for the parameters of an object must always contain data.
- CH 14: For every "ActivityConnect" and ActivityModule (except ActivityCause), provide a connection point to ActivityCause except for input/output connection points.
- CH 15: All inputs and outputs of an object must be connected.

- CH 16: The terminal object has only one input and no output while the initial object has only one output and no input.

- CH 17: The system must allow the reusability of values entered into the simulation or calculated by it and stored in memory.

- CH 18: Objects should have access to parameters entered into the simulation or calculated by it and stored in memory.

- CH 19: The interface for model construction must provide graphical objects in a menu, allowing for their reusability, modification and extensibility.

- CH 20: A logical consequence of CH19 is to provide a minimum configuration of generic objects which can be used to construct all other objects.

5.1.3. Constraints on the simulation

- CH 21: The simulation of a HAD model resulting from the reception of a message from one object to another can only evolve when the message is validated and its content is true.

- CH 22: The reception of a message causes the simultaneous activation of immediately following objects and the deactivation of all immediately preceding objects.

- CH 23: Every object has a unique number

- CH 24 : To represent or describe HAD, the following messages are required:

"Displace", "Duplicate", "Delete", "Modify", "Mark", "Search", "Select", «Read parameter ». Consequently, these methods will be declared as "public" in the source code of the simulator.

It is easy to implement the simulator by applying all of these constraints.

5.2. The Simulator of HAD Models (SIMHAD)

The simulator has been modelled using UML 2 [13], to ensure the extensibility and reuseability of its source code. It is implemented in multithread Java [16]. The design details of the simulator will not be presented in this article. The simulator incorporates six (6) different interfaces, three of which include the model construction interface, the model description interface and the simulation interface.

When the simulation is in progress, a dialog box displays any errors in the model. Such errors may result from the absence of parameter values, inappropriate connectivity of objects or some other violation of a constraint. The dialog box also shows the time that has elapsed since the simulation was launched. A red dot moves from the top of the diagram towards the bottom, to show the order in which the objects are activated. This is the sequential phase of the system. By double-clicking on an object, the

curves representing the continuous-time dynamics of the object are displayed.

Note that the curves represent the operations or methods associated with the object. Figure 12 shows the simulation interface during the simulation of the liquid-level control system. Figure 13 illustrates the simulation of the HAD model of a system.

The curves are plotted by first resolving equation (1), presented in section 4, to give the result,

$$\Rightarrow \Omega(t) = (1 - e^{-\frac{f_r}{J_r} t}) \frac{T_d - c}{f_r} \quad (3)$$

This expresses the speed as a function of time.

The simulator then plots graphs of equations 2 (section 4), 3 and 4.

$$Tr(n) = a.n^2 + b.n + c \quad (4)$$

Equation 4 represents the torque of the motor shaft and load.

The different curves obtainable from a SIMHAD simulation are presented in [14], [15]. For example, by double-clicking on object number 2 of the diagram in figure 12, the results in figure 13 are obtained.

The speed curves obtained from the simulator are consistent with those found in the literature. The simulator also highlights one of the advantages of HAD – encapsulation of the actions and interactions of the hybrid system.

Details of the functionality and implementation of SIMHAD will be the subject of the next article to be published by the authors.

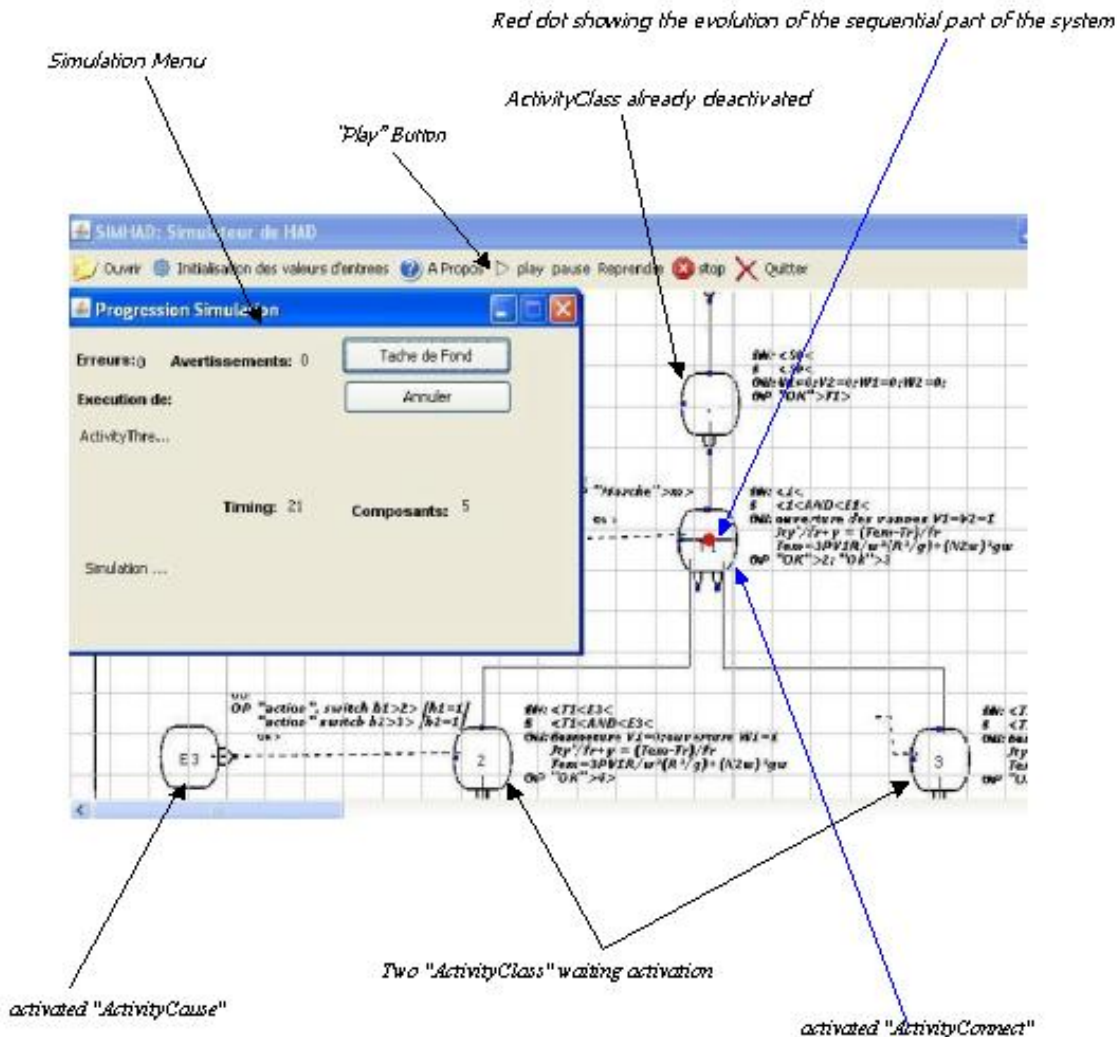


Fig. 12. Simulation Interface showing the liquid-level control system

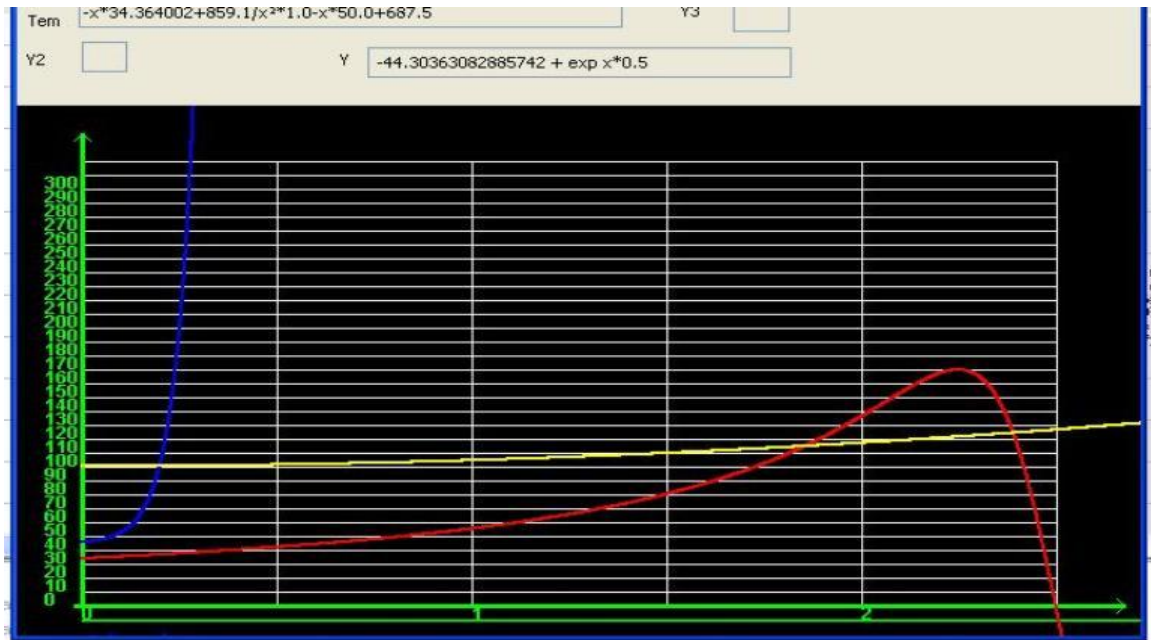


Fig. 13. Curves obtained from SIMHAD

6. CONCLUSIONS AND PERSPECTIVES

The current phase of our research project, described in this paper, has a triple objective :

- Illustrate the functionality of the HAD metamodel as a tool which is specifically adapted to the modeling of hybrid dynamic systems such as the liquid-level control system
- Present the bridges which serve as mechanisms for converting HAD models to UML and Grafcet
- Present SIMHAD – a simulator of HAD models

All of these three objectives have been fulfilled.

The next phase of the research project will focus on the extension of SIMHAD. Two aspects merit particular attention:

- Integration of the bridges within the simulator, to facilitate the automatic generation of Grafcet and Activity Diagrams from a HAD model
- Solution of nonlinear differential equations, to extend the range of continuous-time models which can be processed by the system.

REFERENCES

- [1] Tanyi E., Nkenlifack M., "An extended UML for the modeling of hybrid control systems", in Burnham K.J., Haas O.C.L.(Editors), *Proc. of the sixteenth International Conference on Systems Engineering (ICSE2003)*, Coventry, UK, 9-11 September 2003, Vol.2, pp.681-686, ISBN 0-905949-91.
- [2] Tanyi E., Nkenlifack M., "Hybrid Activity Diagrams: Extending UML for the Modeling of Hybrid Systems", Poster in *ECOOP'03, 17th European Conference on Object -Oriented Programming*, July 21-25, 2003, Darmstadt University of Technology, Germany, <http://www.st.informatik.tu-darmstadt.de:8080/ecoop/posters/index.phtml> - Site Web poster.
- [3] M. Nkenlifack, "Modélisation objet et développement d'un atelier de simulation des automatismes industriels hybrides", PhD Thesis, National Advanced School of Engineering (Ecole Nationale Supérieure Polytechnique), University of Yaounde I, Cameroon, 2004.
- [4] E. Tanyi, M. Nkenlifack, "An object oriented simulation platform for hybrid control systems", *Analysis and Design of hybrid systems (ADHS) 2003, Proc. of the IFAC International Conference*, St. Malo, France, June 16-18 2003, Edited by S.Engell, H. Gueguen&J.Zaytoon, ISBN 0-08-04044094-0.
- [5] T. Noulamo, *Modèle Métier et Architectures Génériques pour la Commande et la Surveillance des Systèmes Dynamiques*, PhD Thesis, Faculty of Sciences, University of Yaounde 1, Cameroon, nov. 2010.
- [6] CEI-IEC (International Electrotechnic Commission), *Grafcet specification language for sequential function charts*, International Standard, IEC 60848, 2002.
- [7] T. Noulamo, E. Tanyi, M. Nkenlifack, J. Lienou, « Domain Specific Model and Generic Architectures for Control and Monitoring of Dynamic Systems », *Advances in Computer Science and Engineering Journal*, Volume 4, Issue 1, Pages 55 - 75 (February 2010), Pushpa Publishing House, India.
- [8] J. Zaytoon, *Systèmes Dynamiques Hybrides, Traitée Systèmes automatisés, Information Commande et Communication*, Hermes, Paris, 2001.
- [9] O. Bouissou, M. Martel, "Analyse Statique par Interprétation Abstraite de Systèmes Hybrides Discrets-Continus", *CEA LIST Laboratoire de Sûreté des Logiciels* 22 septembre 2005.
- [10] H. Brenier, *Métamodèle UML Les spécifications fonctionnelles des automatismes industriels et temps réel*, 303-362, Dunod, Paris, 2001.

- [11] M. Flower, *UML Distilled*, Second edition, Addison-Wesley Longman, Inc, 2000.
- [12] R. David, Alla H., *Du Grafet au Réseaux de Petri, série automatique*, 2em édition revue et augmentée, édition Hermes 1992, 1997 500 pages (271).
- [13] OMG, UML 2.0 Reference Manual, //www.omg.org, 2008.
- [14] L. Domche, "Metamodelle HAD-Grafet, Analyse et Mise en Œuvre dans le cadre de la Commande des Réseaux Electriques : cas du Réseau Sud AES SONEL Cameroun", Bachelor Thesis, Electrical Engineering, IUT FV of Bandjoun, University of Dschang, Cameroon, 2009.
- [15] F. Fokou, "Metamodelle UML-HAD, Analyse et Mise en Œuvre dans le cadre de la Commande des Réseaux Electriques : cas du Réseau Sud AES SONEL Cameroun", Bachelor Thesis, Electrical Engineering, IUT FV of Bandjoun, University of Dschang, Cameroon, 2009.
- [16] C. Delannoy, *Programmer en Java*, Eyrolles, France, 2001.
- [17] T. Wildi and G. Sybille, *Electrotechnique*, 3em edition, DeBoeck Université.